# Introduction to Computing II (ITI 1121) MidTERM EXAMINATION 

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## Identification

Last name: $\qquad$ First name: $\qquad$
Student \#: $\qquad$ Seat \#: $\qquad$ Signature: $\qquad$ Lab Section:

## Instructions

## Marking scheme

1. This is a closed book examination.
2. No calculators, electronic devices or other aids are permitted.
(a) Any electronic device or tool must be shut off, stored and out of reach.
(b) Anyone who fails to comply with these regulations may be charged with academic fraud.

| Question | Maximum | Result |
| ---: | ---: | ---: |
| 1 | 20 |  |
| 2 | 10 |  |
| 3 | 15 |  |
| Total | 45 |  |

3. Write your answers in the space provided.
(a) Use the back of pages if necessary.
(b) You may not hand in additional pages.
4. Write comments and assumptions to get partial marks.
5. Beware, poor hand-writing can affect grades. Do not use a red pen.
6. Do not remove pages or the staple holding the examination pages together.
7. Wait for the signal to start of the examination.

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## Question 1 (20 marks)

For this question, we develop a representation for a Magic Square. In its most basic form, a Magic Square is an $n \times n$ grid filled with the numbers $1,2, \ldots, n^{2}$, such that each row and each column, as well the two main diagonals all have the same sum, called the magic constant $M$, where:

$$
M=\frac{n\left(n^{2}+1\right)}{2}
$$

In the example on the right, $n=3$ and $M=15$.


For this question, you must complete the implementation of the class MagicSquare on page 4. Just like in assignment 1, MagicSquare uses a one-dimensional array to store the values of the grid.
A. (4 marks) In the class declaration on page 4, declare three instance variables:
(a) A reference variable used to designate a one-dimensional array of int values. The designated array will be used to store the values of the grid.
(b) A variable to store the size of the grid, where the size represents both the number of rows and the number of columns of the magic square ( 3 in the example above).
(c) A variable to store the magic constant, as defined above ( 15 in this example).
B. (8 marks) In the class declaration on page 4, implement the constructor. Make sure that your implementation complies with the following guidelines:
(a) The constructor stores the values of this magic square specified by the parameter. As illustrated by the test program on the next page, an object of the class MagicSquare is not affected by subsequent changes to the array of values passed as an argument to the constructor. Herein, you can assume that the the value of the parameter will not be null and the given array forms a square. In other words, the length of the array is a power of 2 for some integer $n \geq 3$.
(b) The constructor calculates and stores the size of the MagicSquare, where the size represents both the number of rows and the number of columns.
(c) Finally, you must compute and store the value of the magic constant.
C. (4 marks) Implement the following three (3) access methods.
(a) Implement the instance method getSize() that returns the size of this MagicSquare, where the size is the number of rows and columns.
(b) Implement the instance method getConstant() that returns the value of the magic constant, as defined above.
(c) Finally, implement the method getValue(int row, int column). The method returns the value stored at location row and column of the grid. The first row and column have index 0 . You can assume that the values will be valid. Be careful, this a two-dimensional coordinate whereas the information is stored in our one-dimensional array.
D. (4 marks) Implement the helper method isMagicDiagonals(). This method returns true if and only if both sums, the sum of the elements on the main diagonal, and the sum of the elements on the main anti-diagonal, are equal to the magic constant. The method is called by the method isMagic(). You are not required to implement the other two methods called by isMagicSquare(). Specifically, you do not have to implement isMagicRows() and isMagic().

The program below shows you the intended use and behaviour for the class MagicSquare.

```
MagicSquare s1, s2;
int[] values = new int[] {1,8,6,3,5,7,4,9,2};
s1 = new MagicSquare(values);
values[0] = 8;
values[1] = 1;
s2 = new MagicSquare(values);
System.out.println(s1);
System.out.println(s1.getSize());
System.out.println(s1.getConstant());
System.out.println(sl.isMagic ());
System.out.println();
System.out.println(s2);
System.out.println(s2.getSize());
System.out.println(s2.getConstant ());
System.out.println(s2.isMagic ());
```

The execution of the above program displays the following on the console:


Reminders: In Java, Math.sqrt(double a) can be used to calculate the square root of a number, whereas Math.pow(double a, double) returns the value of the first argument raised to the power of the second one. You can force types from double to int, if you need to.
public class MagicSquare \{
// Part A. Instance variables
// Part B. Constructor
public MagicSquare (int[] values) \{
// Part C. Access methods
// Part D. isDiagonals()
public boolean isMagic () \{
return isMagicRows () \&\& isMagicColumns() \&\& isMagicDiagonals (); \}
// The source code for the other methods, including isMagicRows() // and isMagicColumns(), is hidden.
private boolean isMagicDiagonals() \{

## Question 2 ( 10 marks)

You must complete the implementation of the class method reverse(String[] a). After a call to this method, the values of the array designated by the parameter a are in the reverse order, as shown in the example below. Your implementation must make use a stack to do the work of reversing the order of the elements. Herein,

- Stack is an interface, with the usual methods: push, pop, and isEmpty;
- StackImplementation is a class that implements the interface Stack. This implementation can store an arbitrarily large number of elements. You don't need to implement this class.

The small Java program below illustrates the expected behaviour.

```
String[] alphabet;
alphabet = new String[] {"alpha", "bravo", "charlie", "delta", "echo"};
System.out. println(Arrays.toString(alphabet));
StringUtils.reverse(alphabet);
System.out.println(Arrays.toString(alphabet));
```

Its execution produces the following output:
[alpha, bravo, charlie, delta, echo]
[echo, delta, charlie, bravo, alpha]
Give your solution in the box provided for this purpose on the following page.
public class StringUtils \{
public $\qquad$
$\qquad$ reverse(String[] a) \{

Stack< $\qquad$ > s;

## Question 3 ( 15 marks)

For this question, you must implement a class called Token. An object of the class Token can either store the reference of String or a primitive value of type int. Accordingly, the class has two constructors, one for each type. Here is a detailed specification of its implementation.
A. (1 mark) Write the class declaration for Token.
B. (3 marks) Declare the necessary instance variables so that an object of the class Token can store the reference of a String. It can store a value of the primitive type int (the value must be stored as an int). Finally, the object must know if it is storing the reference of a String or a value of type int.
C. (2 marks) Give the implementation of the constructor Token(String value). The constructor stores the reference of the object designated by the parameter value. The object must remember that it stores a value of type String.
D. (2 marks) Give the implementation of the constructor Token(int value). The constructor stores the value of the parameter value. The object must remember that it stores a value of type int.
E. (1 mark) Implement the instance method isString() that returns true if this object stores a value of type String, and false otherwise.
F. (2 marks) Implement the instance method toString() that returns a String representation of this object. See below for examples.
G. (4 marks) Implement the class method equals(Token a, Token b) that returns true if the objects designated by the parameters $\mathbf{a}$ and $\mathbf{b}$ are logically equivalent (have the same content) and false otherwise.

```
Token a, b, c;
a = new Token("alpha");
b = new Token("alpha");
c = new Token(42);
System.out.println(a);
System.out.println(b);
System.out.println(c);
System.out.println();
System.out.println("a.isString() is " + a.isString());
System.out.println("c.isString() is " + c.isString());
System.out. println();
System.out.println("Token.equals(a,b) is " + Token.equals(a,b));
System.out.println("Token.equals(b,c) is " + Token.equals(b,c));
System.out.println("Token.equals(c,null) is " + Token.equals(c,null));
```

Token: alpha
Token: alpha
Token: 42
a.isString() is true
c.isString() is false

Token.equals( $a, b$ ) is true
Token.equals(b,c) is false
Token.equals(c,null) is false
Give the implementation of the class Token in the space below.

